

October 10-12, 2023



ALCF Hands-on HPC Workshop

Hands-on Breakout Session

Kokkos / RAJA

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Kokkos

CG Solve: The AXPBY

- Simple data parallel loop: Kokkos::parallel_for
- Easy to express in most programming models
- Bandwidth bound
- Serial Implementation:

```
void axpby(int n, double* z, double alpha, const double* x,  
          double beta, const double* y) {  
    for(int i=0; i<n; i++)  
        z[i] = alpha*x[i] + beta*y[i];  
}
```

Parallel Pattern: for loop

- Kokkos Implementation:

```
void axpby(int n, View<double*> z, double alpha, View<const double*> x,  
           double beta, View<const double*> y) {  
    parallel_for("AXpBY", n, KOKKOS_LAMBDA (const int i) {  
        z(i) = alpha*x(i) + beta*y(i);  
    });
```

String Label: Profiling/Debugging

Execution Policy: do n iterations

Loop Body

Iteration handle: integer index



CG Solve: The Dot Product

- Simple data parallel loop with reduction: Kokkos::parallel_reduce
- Non trivial in CUDA due to lack of built-in reduction support
- Bandwidth bound
- Serial Implementation:

```
double dot(int n, const double* x, const double* y) {  
    double sum = 0.0;  
    for(int i=0; i<n; i++)  
        sum += x[i]*y[i];  
    return sum;  
}
```

Parallel Pattern: loop with reduction

Iteration Index + Thread-Local Red. Varible

- Kokkos Implementation:

```
double dot(int n, View<const double*> x, View<const double*> y) {  
    double x_dot_y = 0.0;  
    parallel_reduce("Dot",n, KOKKOS_LAMBDA (const int i,double& sum) {  
        sum += x[i]*y[i];  
    }, x_dot_y);  
    return x_dot_y;  
}
```



CG Solve: Sparse Matrix Vector Multiply

- Loop over rows
- Dot product of matrix row with a vector
- Example of Non-Tightly nested loops
- Random access on the vector (Texture fetch on GPUs)

```
void SPMV(int nrows, const int* A_row_offsets, const int* A_cols,
          const double* A_vals, double* y, const double* x) {
    for(int row=0; row<nrows; ++row) {
        double sum = 0.0;
        int row_start=A_row_offsets[row];
        int row_end=A_row_offsets[row+1];
        for(int i=row_start; i<row_end; ++i) {
            sum += A_vals[i]*x[A_cols[i]];
        }
        y[row] = sum;
    }
}
```

Outer loop over matrix rows

Inner dot product row x vector



CG Solve: Sparse Matrix Vector Multiply



```
void SPMV(int nrows, View<const int*> A_row_offsets,  
          View<const int*> A_cols, View<const double*> A_vals,  
          View<double*> y,  
          View<const double*, MemoryTraits< RandomAccess>> x) {
```

Enable Texture Fetch on x

```
// Performance heuristic to figure out how many rows to give to a team  
int rows_per_team = get_row_chunking(A_row_offsets);
```

```
parallel_for("SPMV:Hierarchy", TeamPolicy< Schedule< Static > >  
    ((nrows+rows_per_team-1)/rows_per_team,AUTO,8),  
    KOKKOS_LAMBDA (const TeamPolicy<>::member_type& team) {
```

```
    const int first_row = team.league_rank()*rows_per_team;  
    const int last_row = first_row+rows_per_team<nrows? first_row+rows_per_team : nrows;
```

```
    parallel_for(TeamThreadRange(team,first_row,last_row), [&] (const int row) {  
        const int row_start=A_row_offsets[row];  
        const int row_length=A_row_offsets[row+1]-row_start;
```

Row x Vector dot product

```
        double y_row;  
        parallel_reduce(ThreadVectorRange(team,row_length), [&] (const int i, double& sum) {  
            sum += A_vals(i+row_start)*x(A_cols(i+row_start));  
        } , y_row);  
        y(row) = y_row;  
    });  
});  
};
```

Distribute rows in workset over team-threads

Team Parallelism over Row Worksets

Kokkos

```
> git clone https://github.com/kokkos/kokkos.git  
> git clone https://github.com/kokkos/kokkos-tutorials.git  
> cd kokkos-tutorials/Exercises/01/Begin
```

Kokkos

exercise_1_begin.cpp

```
51 #include <sys/time.h>
52
53 // EXERCISE: Include Kokkos_Core.hpp.
54 //           cmath library unnecessary after.
55 // #include <Kokkos_Core.hpp>
56 #include <cmath>
57
58 void checkSizes( int &N, int &M, int &S, int &nrepeat );
```

Kokkos

exercise_1_begin.cpp

```
95 // Check sizes.  
96 checkSizes( N, M, S, nrepeat );  
97  
98 // EXERCISE: Initialize Kokkos runtime.  
99 // Include braces to encapsulate code between initialize and finalize calls  
100 // Kokkos::initialize( argc, argv );  
101 // {  
102  
103 // Allocate y, x vectors and Matrix A:  
104 double * const y = new double[ N ];
```

Kokkos

exercise_1_begin.cpp

```
108 // Initialize y vector.  
109 // EXERCISE: Convert outer loop to Kokkos::parallel_for.  
110 for ( int i = 0; i < N; ++i ) {  
111     y[ i ] = 1;  
112 }  
113  
114 // Initialize x vector.  
115 // EXERCISE: Convert outer loop to Kokkos::parallel_for.  
116 for ( int i = 0; i < M; ++i ) {  
117     x[ i ] = 1;  
118 }  
119  
120 // Initialize A matrix, note 2D indexing computation.  
121 // EXERCISE: Convert outer loop to Kokkos::parallel_for.  
122 for ( int j = 0; j < N; ++j ) {  
123     for ( int i = 0; i < M; ++i ) {  
124         A[ j * M + i ] = 1;
```

Kokkos

exercise_1_begin.cpp

```
108 // Initialize y vector.  
109 Kokkos::parallel_for( "y_init", N, KOKKOS_LAMBDA ( int i ) {  
110     y[ i ] = 1;  
111 } );  
112  
113 // Initialize x vector.  
114 Kokkos::parallel_for( "x_init", M, KOKKOS_LAMBDA ( int i ) {  
115     x[ i ] = 1;  
116 } );  
117  
118 // Initialize A matrix, note 2D indexing computation.  
119 Kokkos::parallel_for( "matrix_init", N, KOKKOS_LAMBDA ( int j ) {  
120     for ( int i = 0; i < M; ++i ) {  
121         A[ j * M + i ] = 1;  
122     }  
123 } );
```

Kokkos

exercise_1_begin.cpp

```
138 // EXERCISE: Convert outer loop to Kokkos::parallel_reduce.  
139 for ( int j = 0; j < N; ++j ) {  
140     double temp2 = 0;  
141  
142     for ( int i = 0; i < M; ++i ) {  
143         temp2 += A[ j * M + i ] * x[ i ];  
144     }  
145  
146     result += y[ j ] * temp2;  
147 }  
148
```

Kokkos

exercise_1_begin.cpp

```
138     Kokkos::parallel_reduce( "yAx", N, KOKKOS_LAMBDA ( int j, double &update ) {  
139         double temp2 = 0;  
140  
141         for ( int i = 0; i < M; ++i ) {  
142             temp2 += A[ j * M + i ] * x[ i ];  
143         }  
144  
145         update += y[ j ] * temp2;  
146     }, result );
```

Kokkos

exercise_1_begin.cpp

```
182  
183 // EXERCISE: finalize Kokkos runtime  
184 // }  
185 // Kokkos::finalize();  
186  
187 return 0;  
188 }
```

Kokkos

Build and Environment

POLARIS

```
> module swap PrgEnv-nvhpc/8.3.3 PrgEnv-gnu  
> module load nvhpc-mixed  
> cd /path/to/kokkos-tutorials/02/Begin  
  
> make KOKKOS_PATH=/path/to/kokkos KOKKOS_DEVICES="Cuda" KOKKOS_ARCH="Ampere80"
```

RAJA

RAJA loop execution has four core concepts

```
using EXEC_POLICY = ...;  
RAJA::RangeSegment range(0, N);  
  
RAJA::forall< EXEC_POLICY >( range, [=] (int i)  
{  
    // loop body...  
} );
```

1. Loop **execution template** (e.g., ‘forall’)
2. Loop **execution policy type** (EXEC_POLICY)
3. Loop **iteration space** (e.g., ‘RangeSegment’)
4. Loop **body** (C++ lambda expression)

Reduction is a common and important parallel pattern

dot product: $dot = \sum_{i=0}^{N-1} a_i b_i$, where a and b are vectors, dot is a scalar

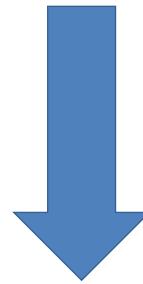
C-style

```
double dot = 0.0;
for (int i = 0; i < N; ++i) {
    dot += a[i] * b[i];
}
```

A RAJA reduction object hides the complexity of a parallel reduction operation

C-style

```
double dot = 0.0;  
for (int i = 0; i < N; ++i) {  
    dot += a[i] * b[i];  
}
```



```
RAJA::ReduceSum< REDUCE_POLICY, double> dot(0.0);
```

RAJA

```
RAJA::forall< EXEC_POLICY >( range, [=] (int i) {  
    dot += a[i] * b[i];  
} );
```

Elements of RAJA reductions...

```
RAJA::ReduceSum< REDUCE_POLICY, DTYPE > sum(init_val);
```

```
RAJA::forall< EXEC_POLICY >(. . . {  
    sum += func(i);  
} );
```

```
DTYPE reduced_sum = sum.get();
```

- A **reduction type** requires:
 - A reduction policy
 - A reduction value type
 - An initial value

Elements of RAJA reductions...

```
RAJA::ReduceSum< REDUCE_POLICY, DTYPE > sum(init_val);
```

```
RAJA::forall< EXEC_POLICY >( . . . {  
    sum += func(i);  
});
```

```
DTYPE reduced_sum = sum.get();
```

Note that you cannot access the reduced value inside a kernel.

- A reduction type requires:
 - A reduction policy
 - A reduction value type
 - An initial value
- **Updating reduction value is what you expect (+=, min, max)**

Elements of RAJA reductions...

```
RAJA::ReduceSum< REDUCE_POLICY, DTYPE > sum(init_val);
```

```
RAJA::forall< EXEC_POLICY >(. . . {  
    sum += func(i);  
});
```

```
DTYPE reduced_sum = sum.get();
```

- A reduction type requires:
 - A reduction policy
 - A reduction value type
 - An initial value
- Updating reduction value is what you expect ($+=$, min, max)
- **After loop runs, get reduced value via 'get' method**

The reduction policy must be compatible with the loop execution policy

```
RAJA::ReduceSum< REDUCE_POLICY, DTYPE > sum(init_val);
```

```
RAJA::forall< EXEC_POLICY >(... {  
    sum += func(i);  
}) ;
```

```
DTYPE reduced_sum = sum.get();
```

An OpenMP execution policy requires an OpenMP reduction policy, similarly for CUDA, etc.

RAJA provides reduction policies for all supported programming model back-ends

```
RAJA::ReduceSum< REDUCE_POLICY, int > sum(0);
```

```
RAJA::seq_reduce;
```

```
RAJA::omp_reduce;
```

```
RAJA::cuda_reduce;
```

```
RAJA::tbb_reduce;
```

```
RAJA::omp_target_reduce;
```

A sample of RAJA reduction policy types.

Note: OpenMP target and HIP reductions are works-in-progress.

RAJA supports five common reductions types

RAJA::ReduceSum<

REDUCE_POLICY, DTTYPE > r(in_val);

RAJA::ReduceMin<

REDUCE_POLICY, DTTYPE > r(in_val);

RAJA::ReduceMax<

REDUCE_POLICY, DTTYPE > r(in_val);

RAJA::ReduceMinLoc<

REDUCE_POLICY, DTTYPE > r(in_val,
in_loc);

RAJA::ReduceMaxLoc<

REDUCE_POLICY, DTTYPE > r(in_val,
in_loc);

Initial
“loc”
values

“Loc” reductions give a loop index where reduced value was found.

A RAJA “Segment” defines a set of loop iterates

- A **Segment** is a set of loop indices to run for a kernel

Contiguous range [beg, end)



Strided range [beg, end, stride)



List of indices (indirection)



Loop iteration spaces are defined by Segments

- A Segment is a set of loop indices to run for a kernel

Contiguous range [beg, end)



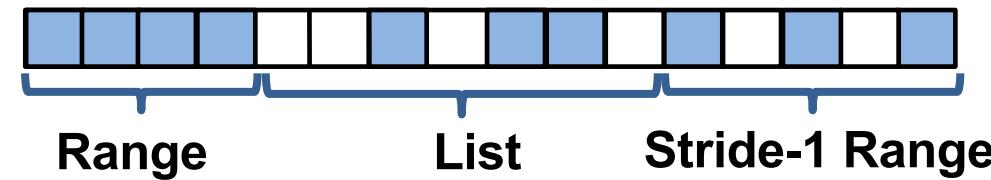
Strided range [beg, end, stride)



List of indices (indirection)



- An **Index Set** is a container of segments (of arbitrary types)



You can run all Segments in an IndexSet in one call to a RAJA loop execution template.

A RangeSegment defines a contiguous sequence of indices (stride-1)

```
RAJA::RangeSegment range( 0, N );
```

```
RAJA::forall< RAJA::seq_exec >( range , [=] (int i)
{
    // ...
} );
```

Runs loop indices: 0, 1, 2, ..., N-1

A RangeStrideSegment defines a strided sequence of indices

```
RAJA::RangeStrideSegment strange1( 0, N, 2 );
```

```
RAJA::forall< RAJA::seq_exec >( strange1 , [=] (int i)
{
    // ...
} );
```

Runs loop indices: 0, 2, 4, ...

Segments also allow negative indices and strides

```
RAJA::RangeStrideSegment strange2( N-1, -1, -1 );
```

```
RAJA::forall< RAJA::seq_exec >( strange2 , [=] (int i)
{
    // ...
} );
```

Runs loop in reverse: N-1, N-2, ..., 1, 0

The RAJA::kernel API is designed for composing and transforming complex kernels

```
using namespace RAJA;
using KERNEL_POL = KernelPolicy<
    statement::For<1, exec_policy_row,
    statement::For<0, exec_policy_col,
    statement::Lambda<0>
>
>
>;
>;
```

```
RAJA::kernel<KERNEL_POL>( RAJA::make_tuple(col_range, row_range) ,
    [=] (int col, int row ) {
```

```
    double dot = 0.0;
    for (int k = 0; k < N; ++k) {
        dot += A(row, k) * B(k, col);
    }
    C(row, col) = dot;
} );
```

Note: lambda expression for inner loop body is the same as C-style variant.

The RAJA::kernel interface uses four basic concepts, analogous to RAJA::forall

1. Kernel **execution template** ('RAJA::kernel')
2. Kernel **execution policies** (in 'KERNEL_POL')
3. Kernel **iteration spaces** (e.g., 'RangeSegments')
4. Kernel **body** (lambda expressions)

Each loop level has an iteration space and loop variable

```
using namespace RAJA;
using KERNEL_POL = KernelPolicy<
    statement::For<1, exec_policy_row,
    statement::For<0, exec_policy_col,
    statement::Lambda<0>
>
>
>;
RAJA::kernel<KERNEL_POL>(
    RAJA::make_tuple(col_range, row_range),
    [=] (int col, int row) {
// ...
});
```

The order (and types) of tuple items and lambda arguments must match.

Each loop level has an execution policy

```
using namespace RAJA;
using KERNEL_POL = KernelPolicy<
    statement::For<1, exec_policy_row,
    statement::For<0, exec_policy_col,
    statement::Lambda<0>
    >
    >
>;
```



```
RAJA::kernel<KERNEL_POL>( RAJA::make_tuple(col_range, row_range),
    [=] (int col, int row) {
// ...
} );
```

‘For’ statement integer parameter indicates tuple item it applies to: ‘0’ → col, 1’ → row.

To transform the loop order, change the execution policy, not the kernel code

```
using KERNEL_POL = KernelPolicy<
```

```
    statement::For<1, exec_policy_row,  
    statement::For<0, exec_policy_col,
```

```
    ...
```

```
>;
```

'For' statements
are swapped.

Outer row loop (1),
inner col loop (0)

```
using KERNEL_POL = KernelPolicy<
```

```
    statement::For<0, exec_policy_col,  
    statement::For<1, exec_policy_row,
```

```
    ...
```

```
>;
```

Outer col loop (0),
inner row loop (1)

This is analogous to swapping for-loops in a C-style implementation.

RAJA::KernelPolicy constructs comprise a simple DSL that relies only on standard C++11 support

- A KernelPolicy is built from “Statements” and “StatementLists”
 - A **Statement** is an action: execute a loop, invoke a lambda, synchronize threads, etc. ,

For<0, exec_pol, ...>

Lambda<0>

CudaSyncThreads

- A **StatementList** is an ordered list of **Statements** processed as a sequence; e.g.,

```
For<0, exec_policy0,  
     Lambda<0>,  
     For<2, exec_policy2,  
           Lambda<1>  
     >  
   >
```

A RAJA::KernelPolicy type is a StatementList.

RAJA

```
> git clone --recursive https://github.com/llnl/raja.git  
> cd raja/exercises/tutorial_halfday
```

RAJA

ex1_vector-addition.cpp

```
105  /// EXERCISE: Implement the vector addition kernel using a RAJA::forall  
106  /// method and RAJA::seq_exec execution policy type.  
107  ///  
108  /// NOTE: We've done this one for you to help you get started...  
109  ///  
110  
111  using EXEC_POL1 = RAJA::seq_exec;  
112  
113  RAJA::forall< EXEC_POL1 >(RAJA::RangeSegment(0, N), [=] (int i) {  
114      c[i] = a[i] + b[i];  
115  });  
116  
117  checkResult(c, c_ref, N);
```

RAJA

ex1_vector-addition.cpp

```
128 std::cout << "\n Running RAJA SIMD vector addition...\n";
129
130 /**
131  * TODO...
132 */
133 /**
134  * EXERCISE: Implement the vector addition kernel using a RAJA::forall
135  * method and RAJA::simd_exec execution policy type.
136 */
137 checkResult(c, c_ref, N);
```

RAJA

ex1_vector-addition.cpp

```
128 std::cout << "\n Running RAJA SIMD vector addition...\n";
129
130 using EXEC_P0L2 = RAJA::simd_exec;
131
132 RAJA::forall< EXEC_P0L2 >(RAJA::RangeSegment(0, N), [=] (int i) {
133     c[i] = a[i] + b[i];
134 });
135
136 checkResult(c, c_ref, N);
```

RAJA

ex1_vector-addition.cpp

```
191 std::cout << "\n Running RAJA OpenMP multithreaded vector addition...\n";
192
193 /**
194  */// TODO...
195 /**
196  */// EXERCISE: Implement the vector addition kernel using a RAJA::forall
197  *///             method and RAJA::omp_parallel_for_exec execution policy type.
198 /**
199
200 checkResult(c, c_ref, N);
```

RAJA

ex1_vector-addition.cpp

```
191 std::cout << "\n Running RAJA OpenMP multithreaded vector addition...\n";
192
193 using EXEC_P0L4 = RAJA::omp_parallel_for_exec;
194
195 RAJA::forall< EXEC_P0L4 >(RAJA::RangeSegment(0, N), [=] (int i) {
196     c[i] = a[i] + b[i];
197 });
198
199 checkResult(c, c_ref, N);
```

RAJA

ex1_vector-addition.cpp

```
213 std::cout << "\n Running RAJA CUDA vector addition...\n";
214
215 /**
216  * TODO...
217 */
218 /**
219  * EXERCISE: Implement the vector addition kernel using a RAJA::forall
220  * method and RAJA::cuda_exec execution policy type.
221 */
222 checkResult(c, c_ref, N);
```

RAJA

ex1_vector-addition.cpp

```
43 #if defined(RAJA_ENABLE_CUDA)
44 const int CUDA_BLOCK_SIZE = 256;
45 #endif
{...}
213 std::cout << "\n Running RAJA CUDA vector addition...\n";
214
215 using EXEC_P0L5 = RAJA::cuda_exec<CUDA_BLOCK_SIZE>;
216
217 RAJA::forall< EXEC_P0L5 >(RAJA::RangeSegment(0, N),
218                           [=] RAJA_DEVICE (int i) {
219     c[i] = a[i] + b[i];
220 });
221
222 checkResult(c, c_ref, N);
```

RAJA

Build and Environment

POLARIS

```
> module swap PrgEnv-nvhpc/8.3.3 PrgEnv-gnu
> module load nvhpc-mixed cmake
> cd /path/to/raja
> mkdir build
> cd build
> cmake -DCMAKE_BUILD_TYPE=Release -DCMAKE_CXX_COMPILER=g++ -DCMAKE_C_COMPILER=gcc
      -DCUDA_COMMON_OPT_FLAGS="-restrict -arch sm_80 --expt-extended-lambda"
      -C ../../host-configs/ubuntu-builds/nvcc_gcc_X.cmake
      -DENABLE_CUDA=On -DRAJA_ENABLE_EXAMPLES=On ..
> Make -j 16
```

